

Design Limitations of Langeven Transducers With PZT8, PZT4, and PMN-PZT Stacks

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Agenda

- **Nonlinear Behavior of Langeven Transducers**
 - Overview of Mathieson (Glasgow University Paper)
 - The Influence of Piezoceramic Stack Location
- **Material Properties & Analysis Tools**
 - PZT4, PZT8, PMN-PZT (Single Crystal)
 - Computer Model Using PiezoTran : Acoustic Transmission Line Theory
- **Designs Limited by Reserve Power**
 - Coupling Coefficient,
 - Voltage
- **Designs Limited by Heat**
 - Piezo Stack Cyclic Stress

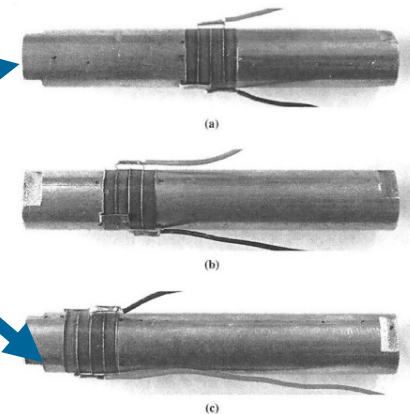
Scope

- Mathieson

- Three Stack Geometries
- Four 10mm PZT4 Rings
- Longitudinal Bending and Torsion Modes of Vibration
- Jump / Hysteresis amplitude plots Vs Volts 1 to 50 VRMS

- Reduced Scope of this Presentation

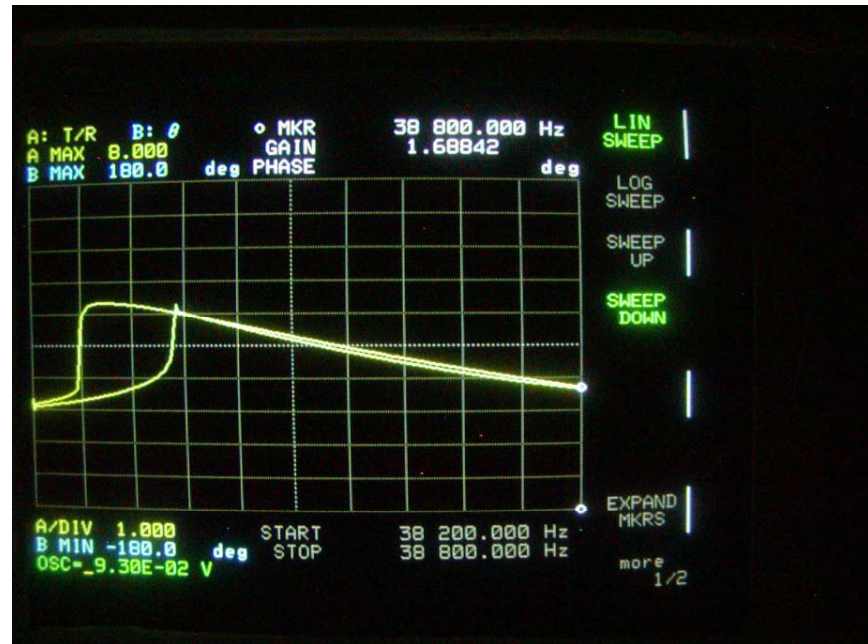
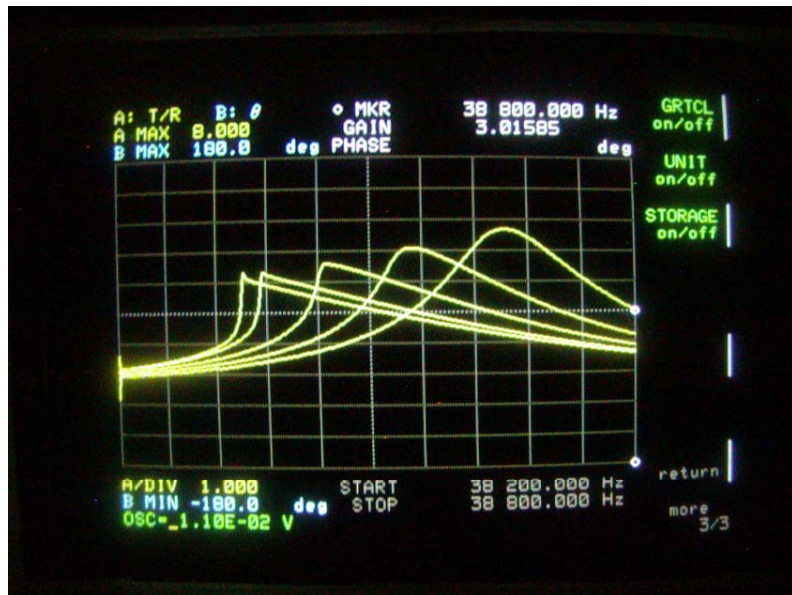
- First Longitudinal Mode of Vibration
- Two Design Geometries



Non Linear Behavior

40 kHz Dumbbell Transducer with 20 MPa bias-stress

- Piezo Innovations Measurement Method
 - HP Impedance/Gain Phase Analyzer 4194A
 - Transfer Function Mode
 - Instruments Inc.L6 or Krohn-Hite 7500 Constant Voltage Amplifier



Material Properties

Inputs For PiezoTran Transducer Analysis Software

Material	k_{33}	Q	E_{33}^T	g_{33}	T_c
PZT 4	0.71	500	1300	24.5	328
PZT 8	0.64	1000	1000	25	300
PMN-PZT	0.93	100	4850	35.6	211

Note: Usage temperature range is typically limited to $\frac{1}{2} T_c$

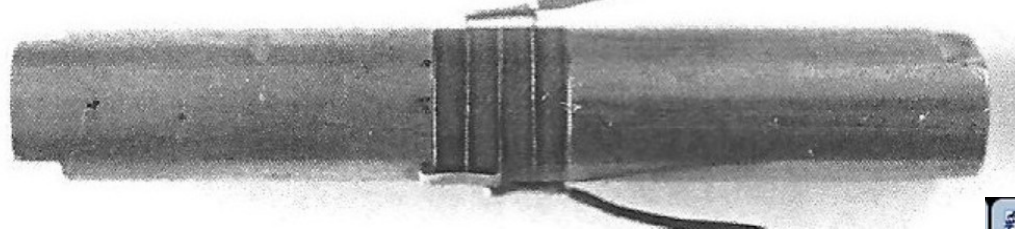
k_{33} is the measure of the ability of thickness mode piezo ceramic stacks to convert electrical energy into mechanical energy

Material	Young's Mod 10^3 MPa	Q*	Density Kg/m ³	Sound Velocity m/s
Titanium 6 al4v	117	20,000	4500	4916
Aluminum2014A-T6	74	10,000	2800	5141
Stainless Steel 316	210	7,000	7750	5200
Beryllium Copper	127		8300	3911
Brass	95		8500	3343
Alumina	240		3300	8528
Tungsten	400		17100	4836

* Typical Q values can be determined from Wuchinich paper entitled :A practical evaluation of harmonic elastic power loss in substantially strained structures

PiezoTran Transducer Analysis

- Acoustic Transmission Line Theory



PiezoTran (by Piezo Innovations)

File Model Analysis Results Help

Model File: L1 PZT4

Analysis Settings: Start Freq. 24000, Stop Freq. 32000, Freq. Step 5, P-P Voltage 2.828, RLoss 24.5

Model Description: 1 1 ratio

Piezo Properties	OD	ID	Thickness	Tan Delta	G33	K33T	S33D
	10	5	2	0.015	0.022	1470	8.53E-12

Transducer Assembly

Type	OD Front	OD Rear	ID	Length	Radius	Elements	Material	Density	c
▶ Rod	10	0	3	25.7	0	46	Brass	8500	3343
Anchor Point	0	0	0	0	0	0		0	0
Piezo Stack	0	0	0	8.0599999	0	4		0	0
Rod	10	0	3	25.7	0	46	Brass	8500	3343

Transducer Assembly => Total Length (mm): 59.46 Selected Component: 1 of 4 Distance from Tip (mm): 25.7

Center Bolt Assembly

Type	OD Front	OD Rear	ID	Length	Radius	Elements	Material	Density	c
▶ Rod	3.5	0	0	10	0	10	Stainless Steel 316	7750	5200

Center Bolt Assembly => Total Length (mm): 10 Selected Component: 1 of 1 Distance from Tip (mm): 10

Piezo Properties Editor

Piezo Ring Properties

OD: 10 ID: 5 Thickness: 2

Material: Navy Type I Density: 7600

Tan Delta: 0.015 G33: 0.022

S33D: 8.53E-12 K33T: 1470

Electrode Properties

Thickness: 0.01 Density: 8000 Velocity of Sound: 5000

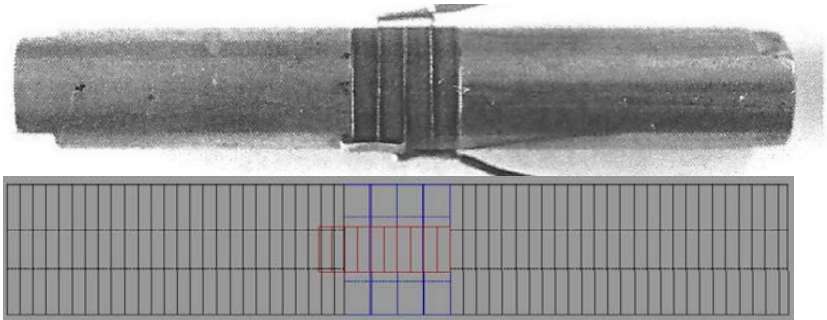
Joint Properties

Thickness: 0.001 Density: 244 Velocity of Sound: 2000

Include Electrodes/Joints at Stack Ends

Apply Properties Close Editor

PiezoTran Output



```

L1 PZT4.ptr_results - Notepad
File Edit Format View Help
Description 1 1 ratio
Resonant Frequency = 26390.0 -----
Maximum Conductance = 0.003797
Anti-Resonant Frequency = 28170.0
Maximum Resistance = 60802
Q = 129.5056 -----
RLoss = 24.50
Coupling Coefficient (K) = 0.3497 -----
Low Frequency (1000 Hz) Capacitance = 1.4214E-009
Maximum Tip Displacement = 2.1227E-007 -----
Applied voltage (P-P) = 2.8280
Applied voltage (RMS) = 1.0000 -----
Power (watts) = 0.0038
Real Current (amps) = 0.0038
    
```

Mathieson Measured Values

Resonant Frequency = 26576

Q = 255

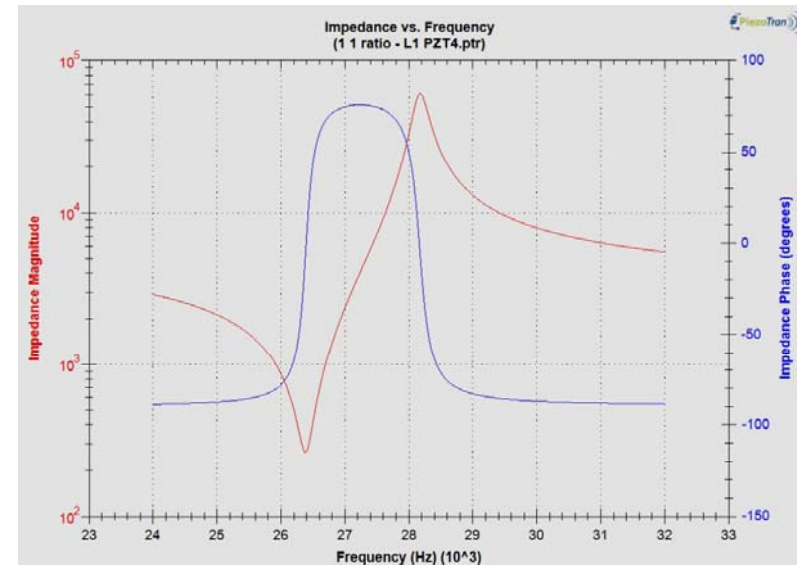
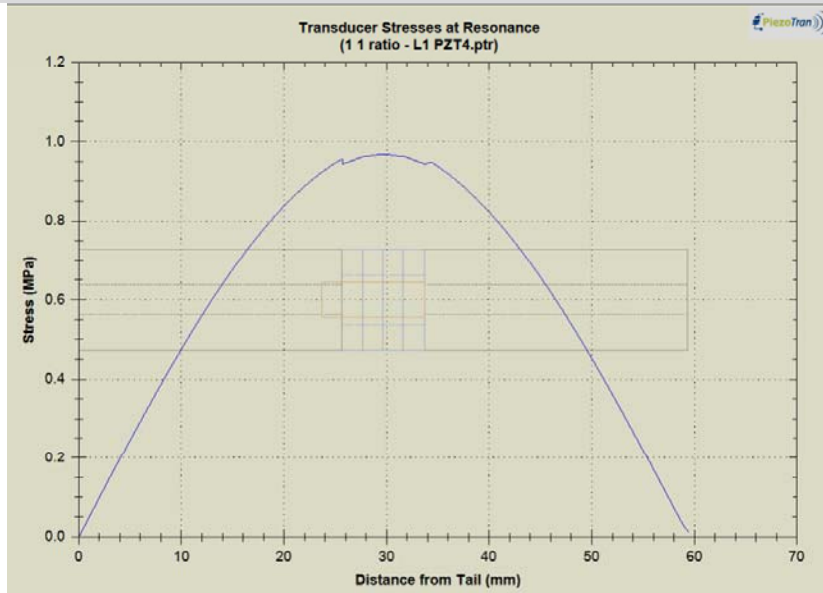
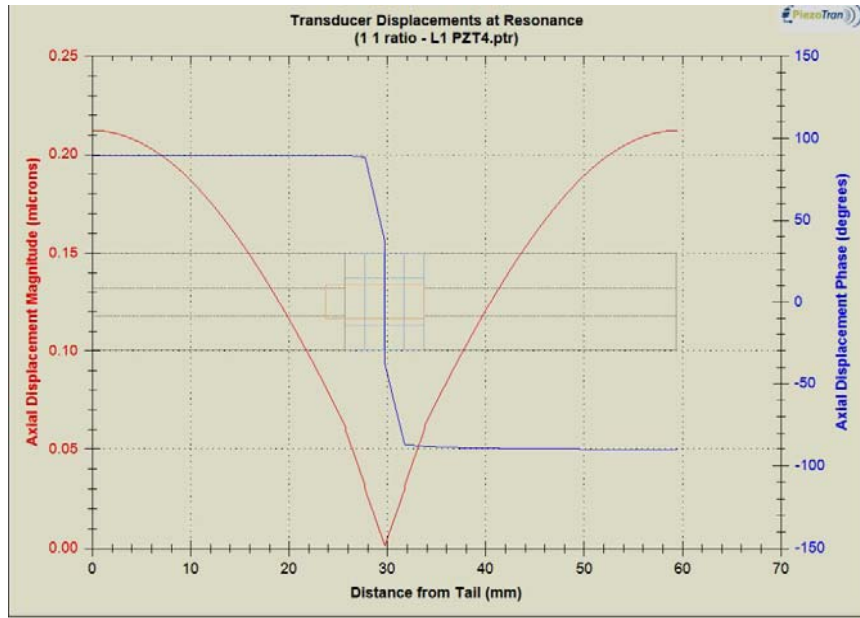
k eff = 0.351

Tip Displacement = 0.2 microns

Applied Voltage 1.0 RMS



Piezotran Outputs



Reserve Power Index (IEC 6147)

- **Scope**

- Ultrasonic Systems Operating in 20 kHz to 60 kHz
- Typically Used to Fragment tissue and bone
- Symmetrical $\frac{1}{2}$ wave transducer with 5 Variable Gain Horns

- **Definition**

- Ratio Of Maximum Electrical Power to Quiescent Electrical Power
 - A measure of How Much “Extra” Power is Available to Maintain a Constant Tip Excursion Amplitude Under Various Load Conditions

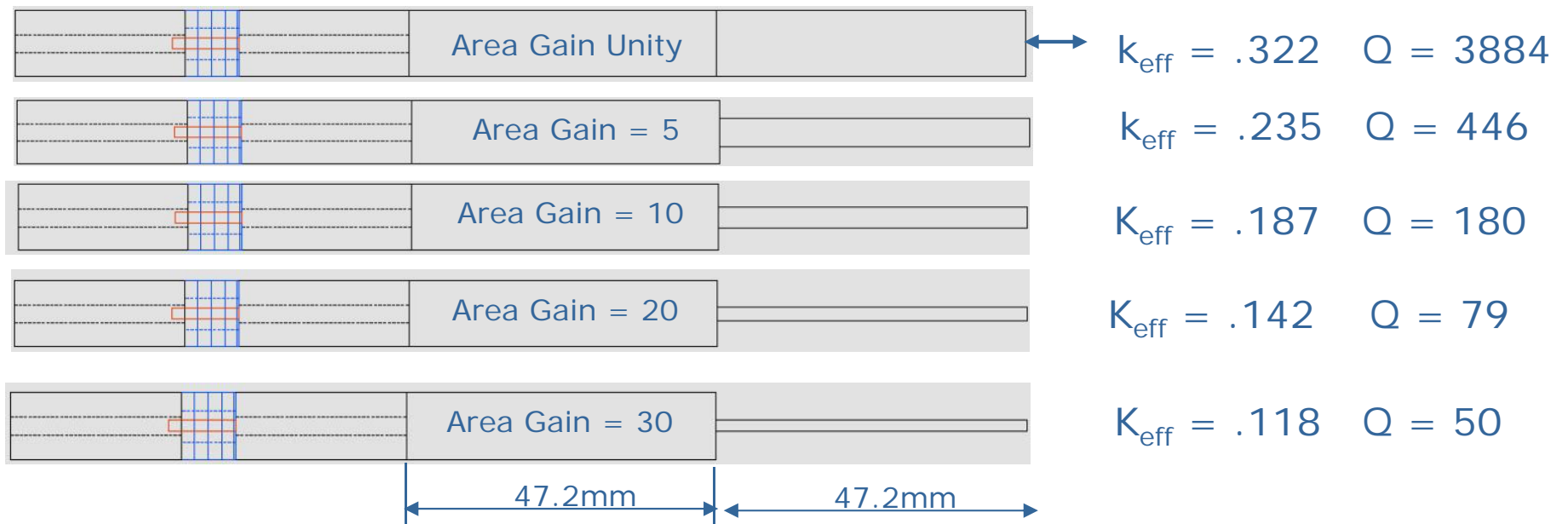
- **Illustrative Example (Using PiezoTran)**

- Assumptions
 - Control System is Voltage Limited to 800 Vp-p
 - Tip Displacement = 62 μm p-p
 - Power = 13 watts
 - $R_{\text{loss}} = 1$ Tip loading condition
- Output
 - Impedance Plots that Illustrate the Importance of Coupling Coefficient

Illustrative Examples

5 Horn Geometries

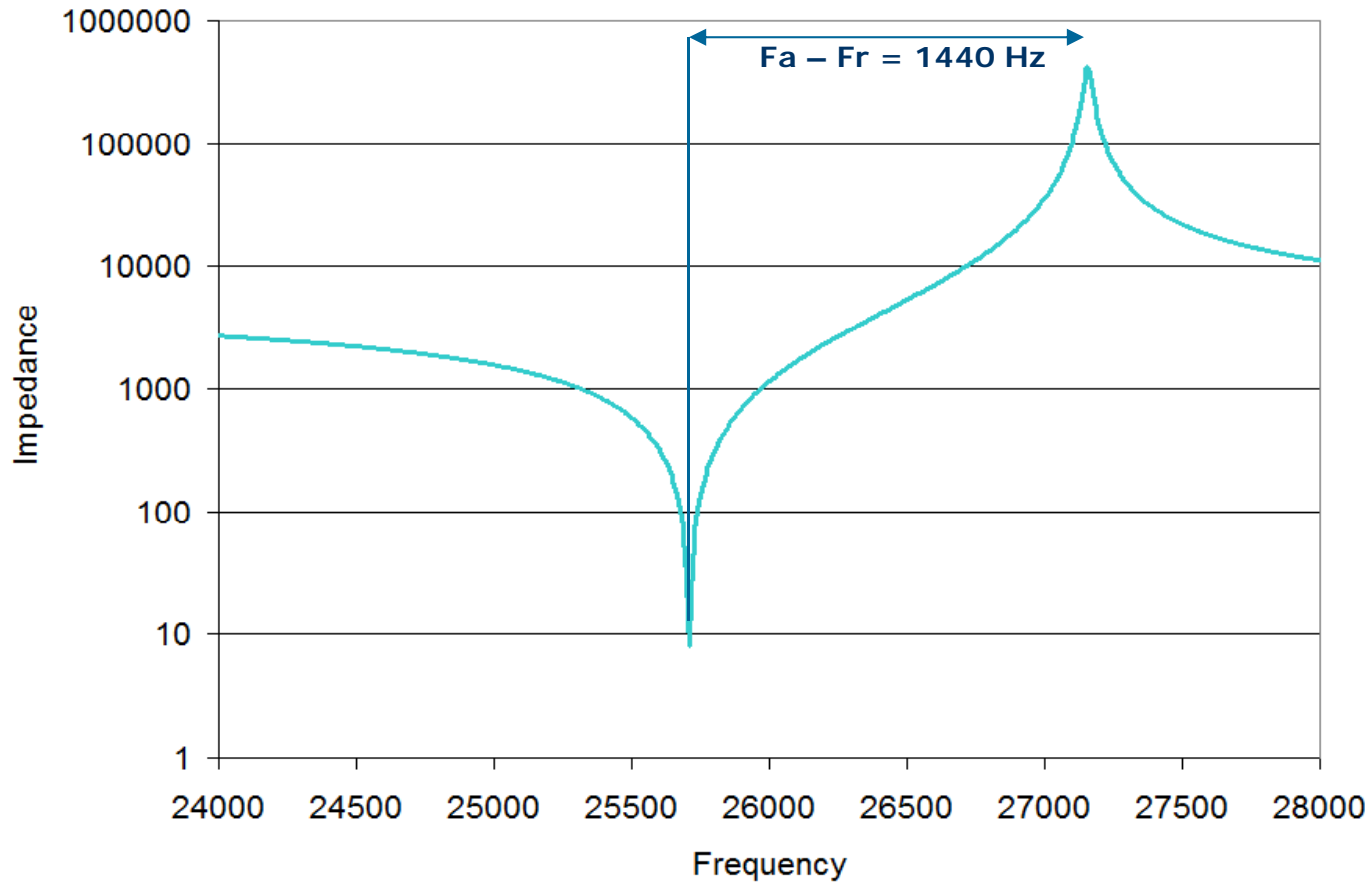
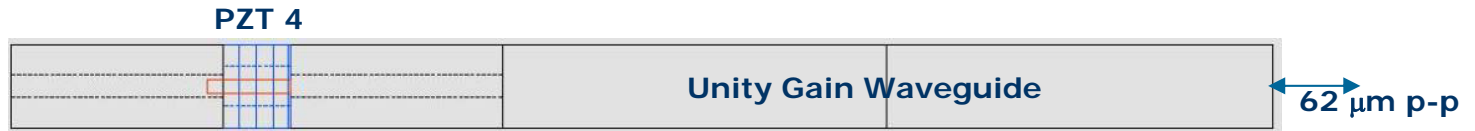
- Resonant Frequency Constant at 26 kHz
- Tip Displacements Constant at 62 μm p-p
- Constant Tip Load Rloss = 1
- Power Constant at 13 Watts



Titanium horns Velocity $c = 4916$ m/s

Unity Gain Horn

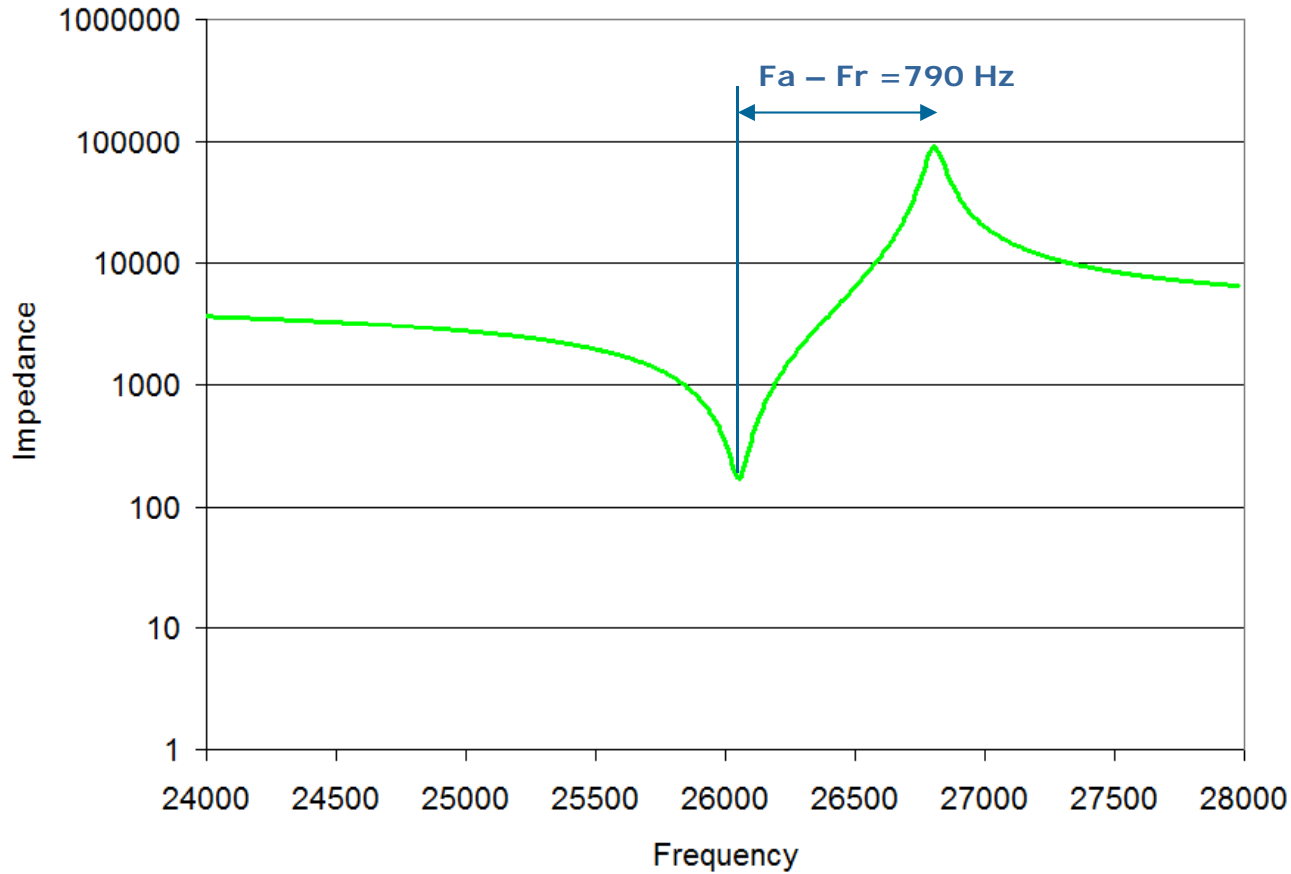
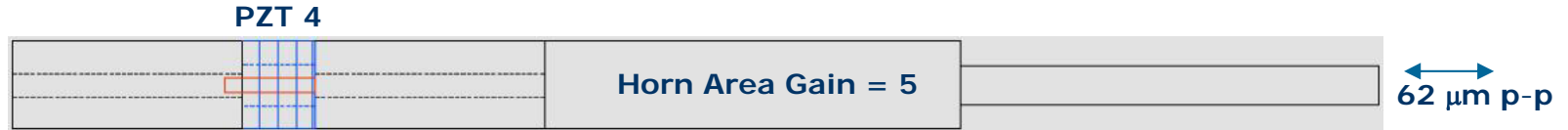
$$k_{\text{eff}} = 0.322$$



$Z_{mn} = 9 \text{ Ohms}$
Phase = + 2.8 °
Volts p-p = 30

Horn Area Gain = 5

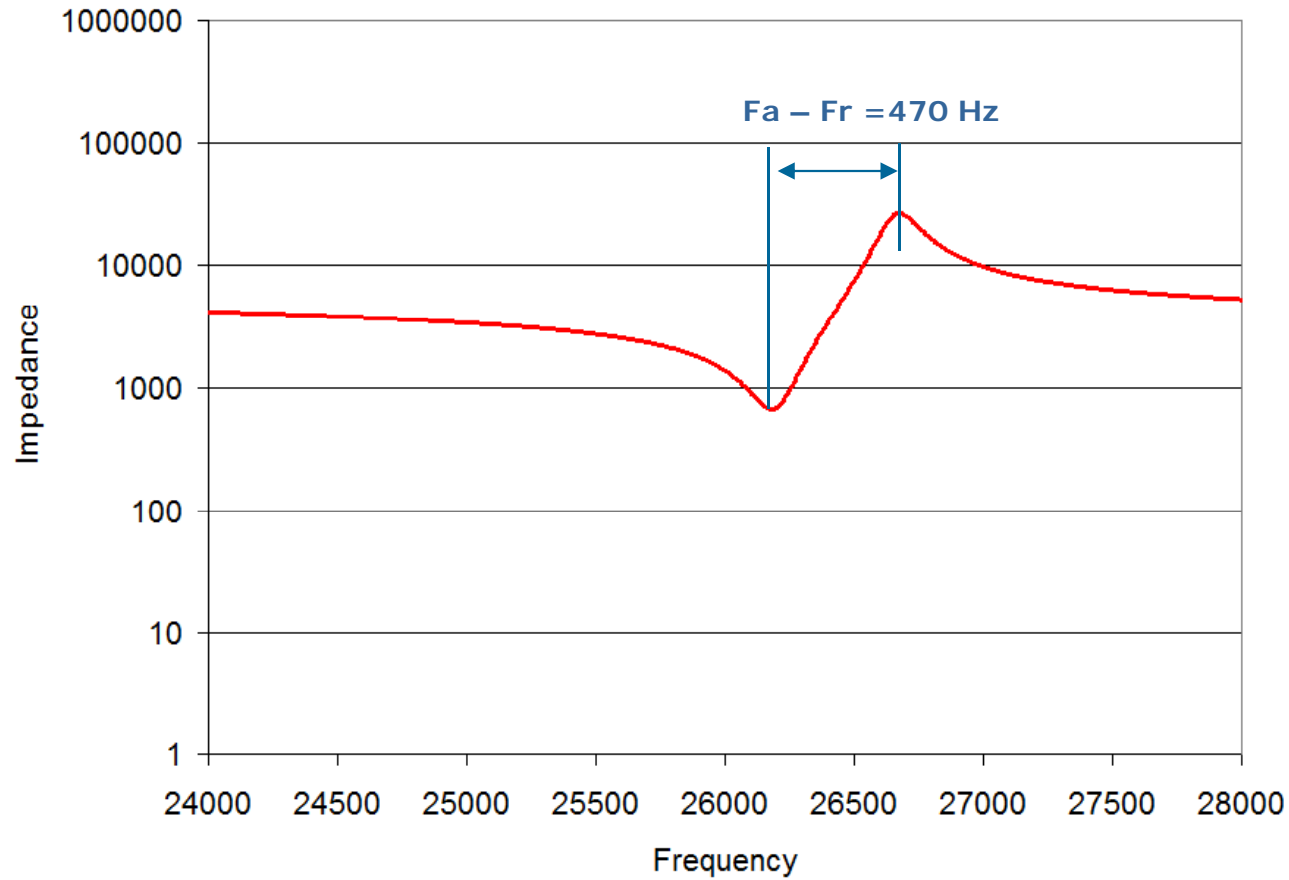
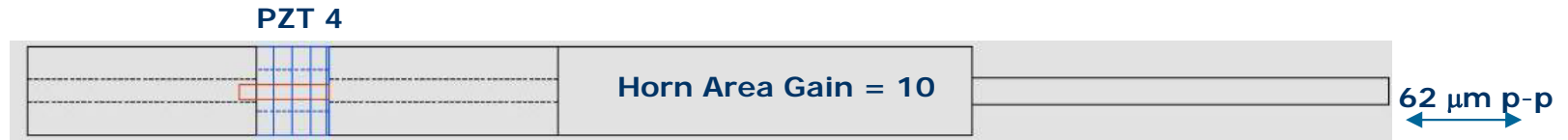
$$k_{\text{eff}} = 0.235$$



$Z_{mn} = 171 \text{ Ohms}$
Phase = -7.6°
Volts p-p = 133

Horn Area Gain = 10

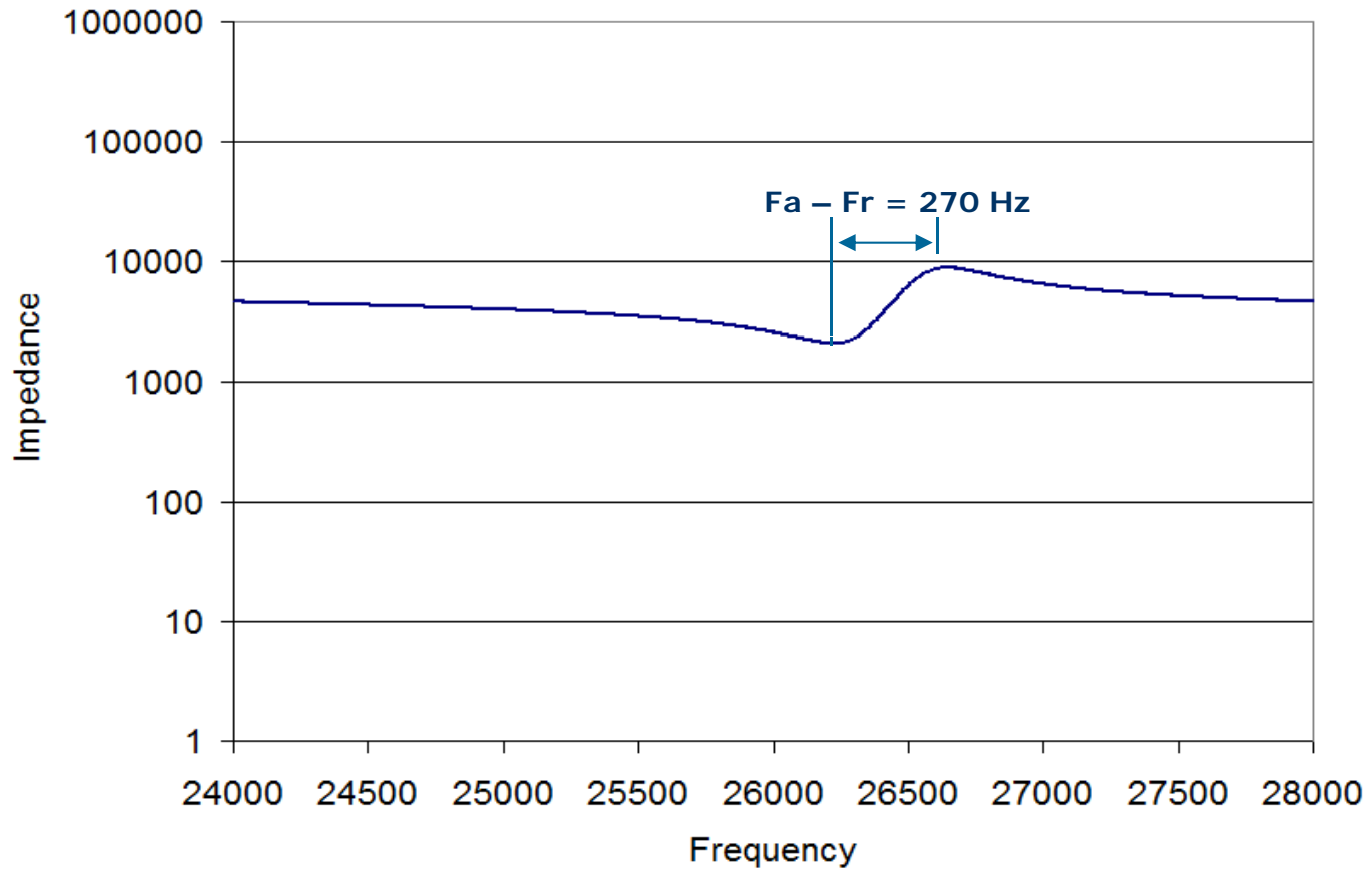
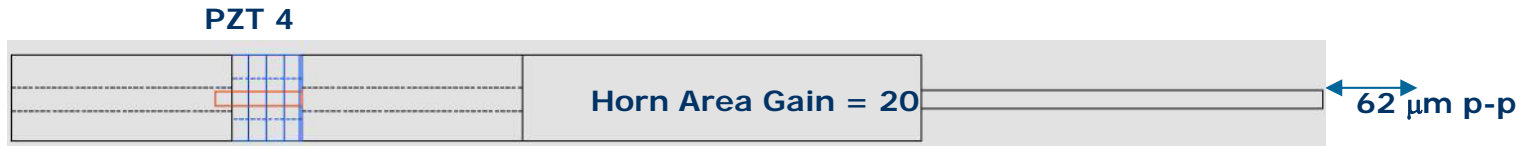
$$k_{\text{eff}} = 0.187$$



$Z_{mn} = 664 \text{ Ohms}$
Phase = -19°
Volts p-p = 266

Horn Area Gain = 20

$$k_{\text{eff}} = 0.142$$

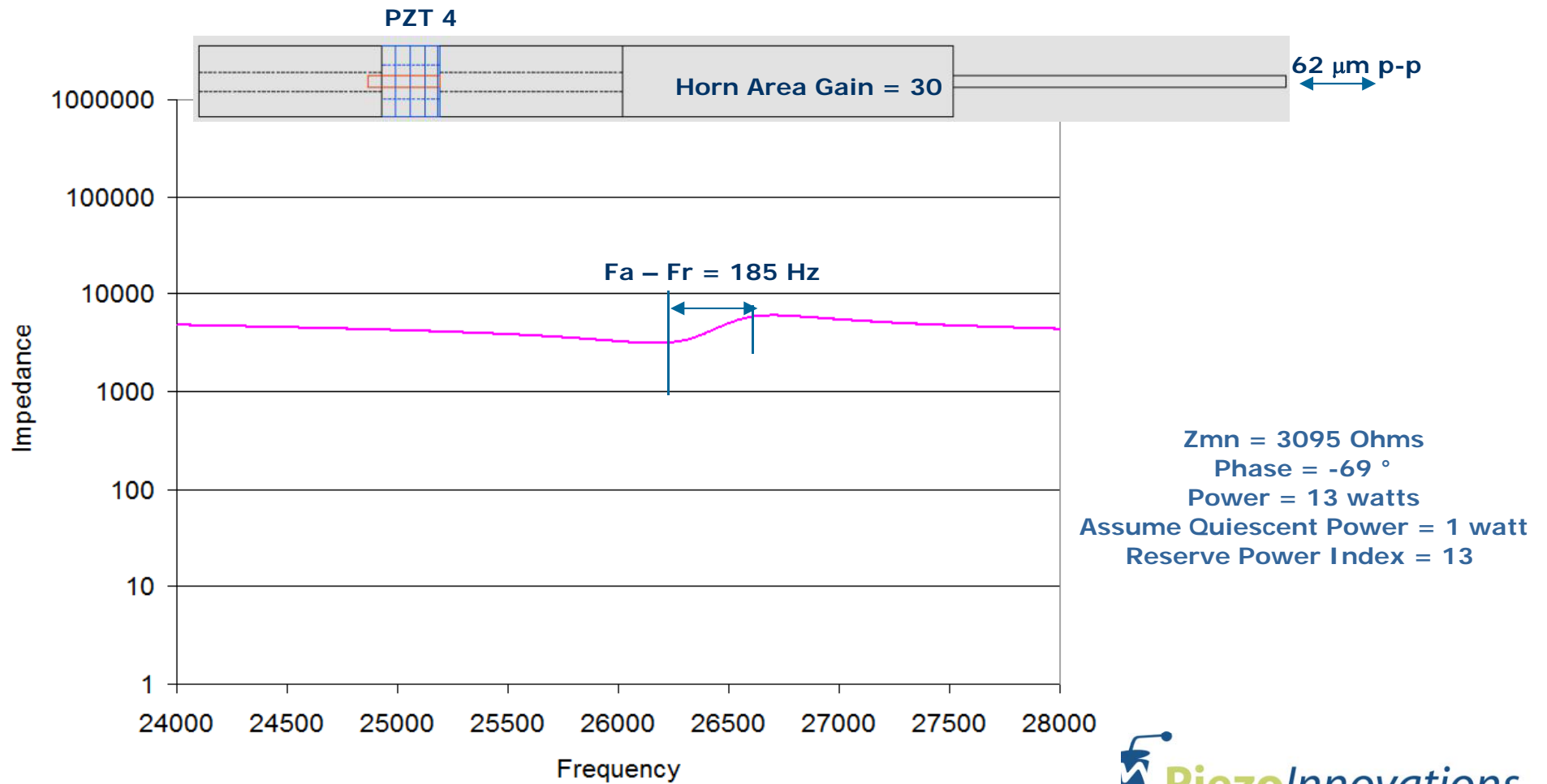


$Z_{mn} = 2082 \text{ Ohms}$
Phase = -50°
Volts p-p = 533

Horn Area Gain = 30

$k_{\text{eff}} = 0.118$

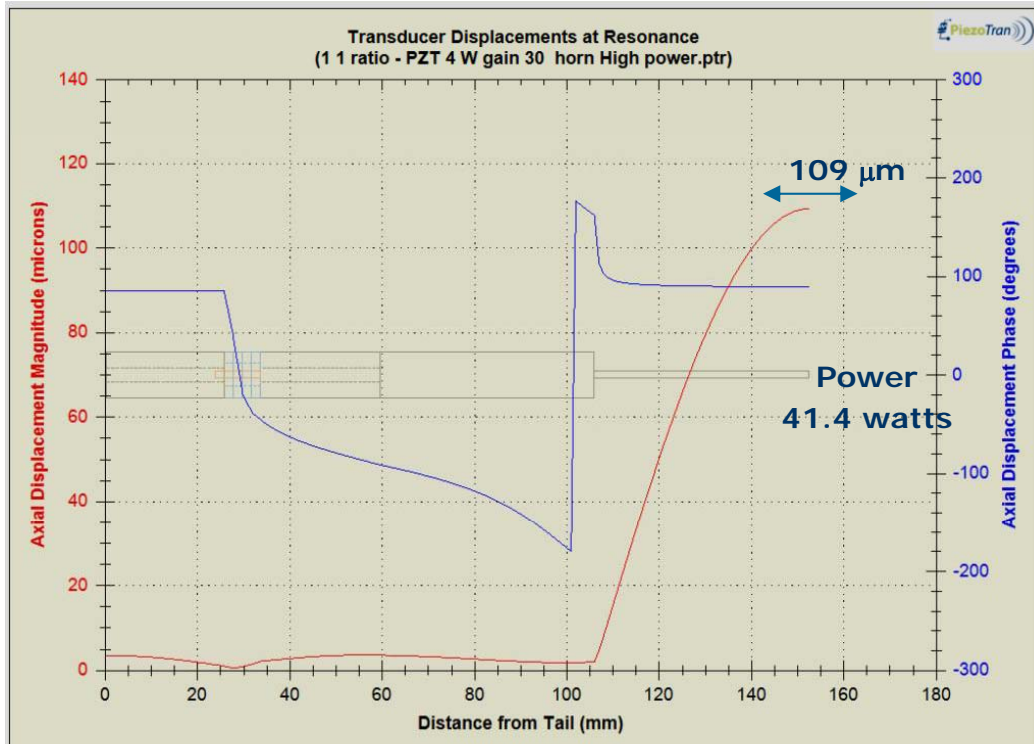
Voltage Limited by Control System 800 Vp-p



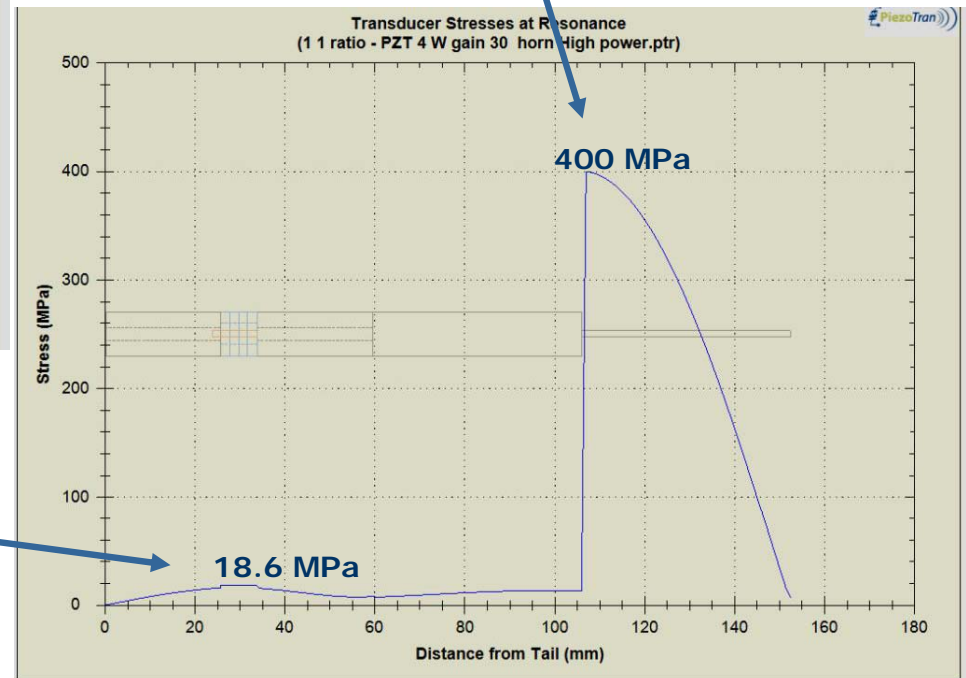
Horn Area Gain = 30

$$k_{\text{eff}} = 0.118$$

Assume Voltage Limit Can be Increased to 500 Vrms (1414 Vp-p)



Potential Design Limitation
Fatigue Limit
Titanium 6Al-4V
390 MPa

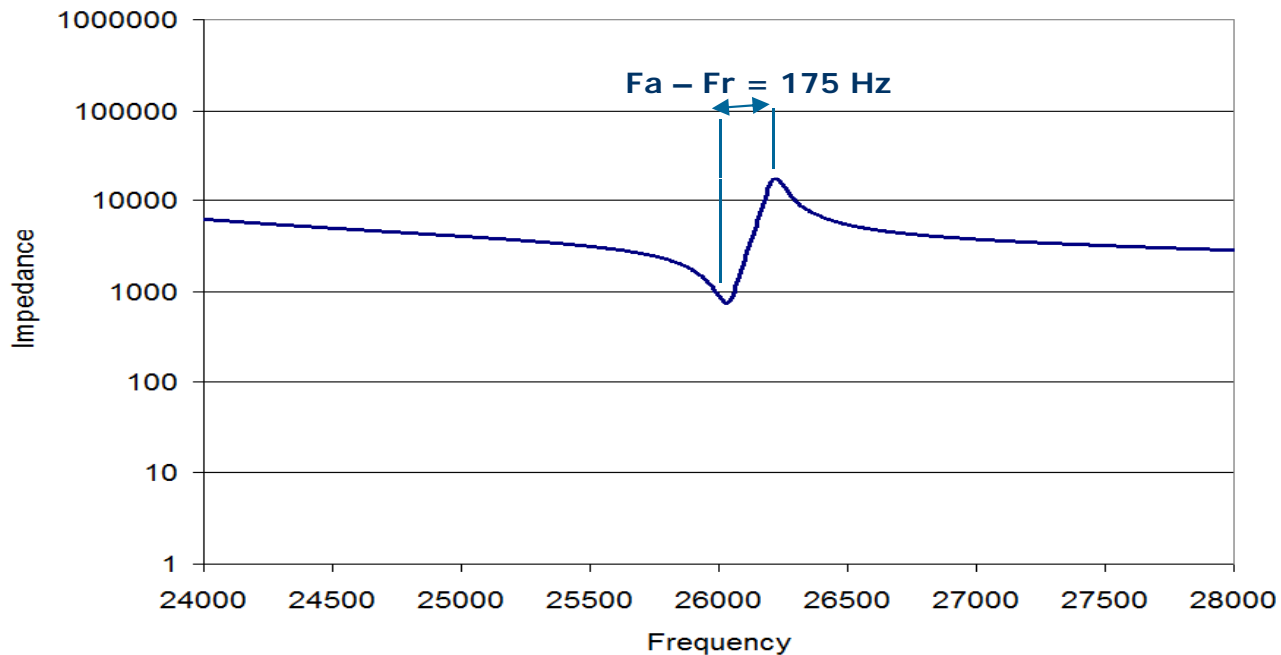
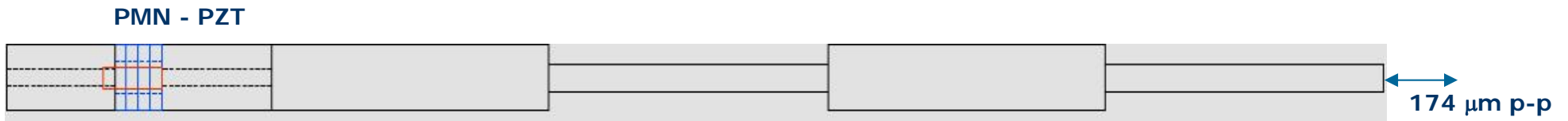


Piezo Stack Cyclic Stress
18.6 MPa
Needs to be < 35.9 MPa to Prevent Heating

Change to PMN-PZT

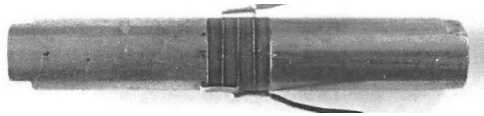
$$k_{\text{eff}} = 0.115$$

- Single Stage Horn (Not Practical)
 - Gain = 87 Minor Diameter = 1.07 mm
- Dual Stage Horn



$Z_{mn} = 751 \text{ Ohms}$
Phase = - 22 °
Volts p-p = 800
Power = 102 watts
Quiescent Power = 2 watts
Reserve Power Index = $102/2 = 51$

Heat Limited Performance

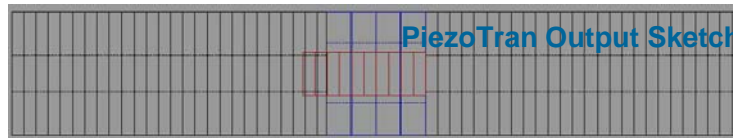
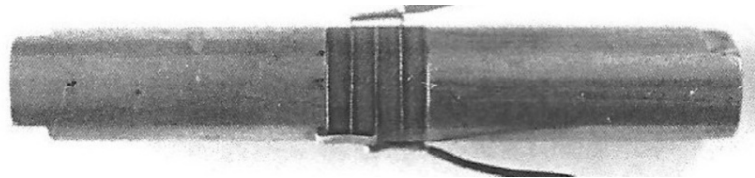


- **Experimental Data**
 - PZT 8 & PZT4 Dumbbells Like this
 - Manually Tuned for Resonance Frequency
 - Air Cooled
 - Stabilize at Approximately 41 ° C* after 10 Minutes
 - Power Manually Adjusted to 1.2 Watts
 - Each Piezo Ring Dissipates approximately 250 mWatts
 - Each End Mass Dissipates 100 mWatts (Includes Joints)

* IEC 60601: applied parts that have localized heating exceeding 41°C must be assessed in risk management

Theory

Heat Limited Designs



$$P_r(\text{thin element}) = \frac{\omega \sigma_M^2 IS}{2QE}$$

P_r = Power loss (heat)

C = sound velocity

E = Youngs modulus

σ_M = peak cyclic stress

S = cross section area

l = length of thin element

PMN-PZT = 80*

PZT 8 = 380*

PZT 4 = 250*

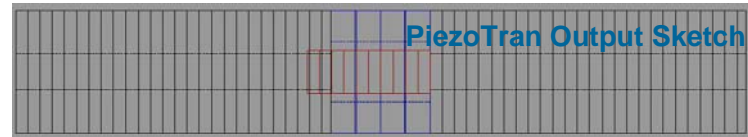
Q : Defined as the ratio of the energy stored to that lost per cycle multiplied by 2π

*Note: Published values of piezo Q relate to test samples

Actual values used based on dumbbell experimental data

Heat Limited Designs

Power Required to Heat Transducer to 41 °C



- Four Ring Designs PZT8 & PZT4

- Each Piezo Ring 250 mWatts
- Each Brass End Mass 100 mWatts

- Four Ring Design 7/8 Configuration PMN-PZT

- Ring (1) 319 mWatts Ring (2) 281 mWatts
- Ring (3) 219 mWatts Ring (4) 145 mWatts



- Two Ring Design PMN-PZT

- Each Ring 300 mWatts (Increased to Compensate For End Mass Conduction)

- One Ring Design PMN-PZT

- Ring (1) 364 mWatts (Increased to Compensate For End Mass Conduction)

Method

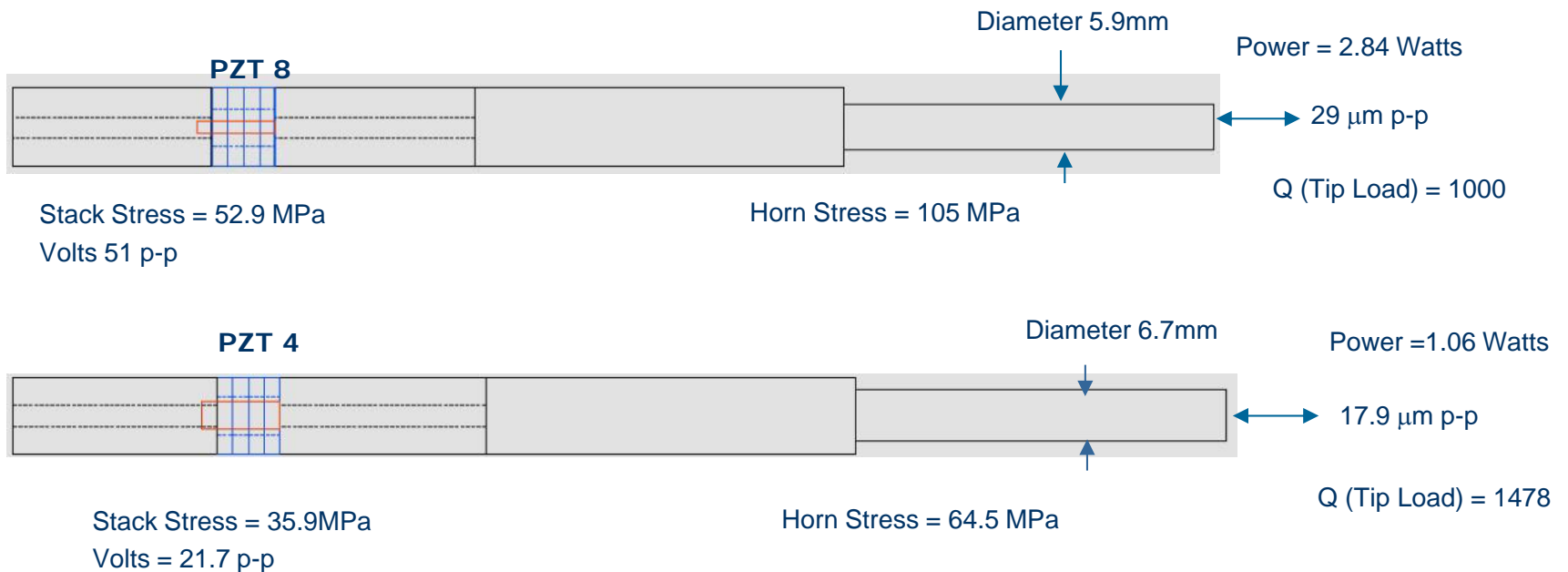
$$P_r(\text{thin element}) = \frac{\omega \sigma_M^2 l S}{2QE}$$

- PiezoTran Output
 - Paste Text Output to Excel Spread Sheet
 - Adjust Accumulated P_r To Coincide With Heat Related Power
 - Determine Corresponding Max p-p Nodal Stress
- PiezoTran Input
 - Adjust PiezoTran Voltage to Corresponding Nodal Stress Value
- PiezoTran Output
 - Keff, Volts p-p, Power, Stack Stress, Horn Stress

PZT8 Comparison With PZT4

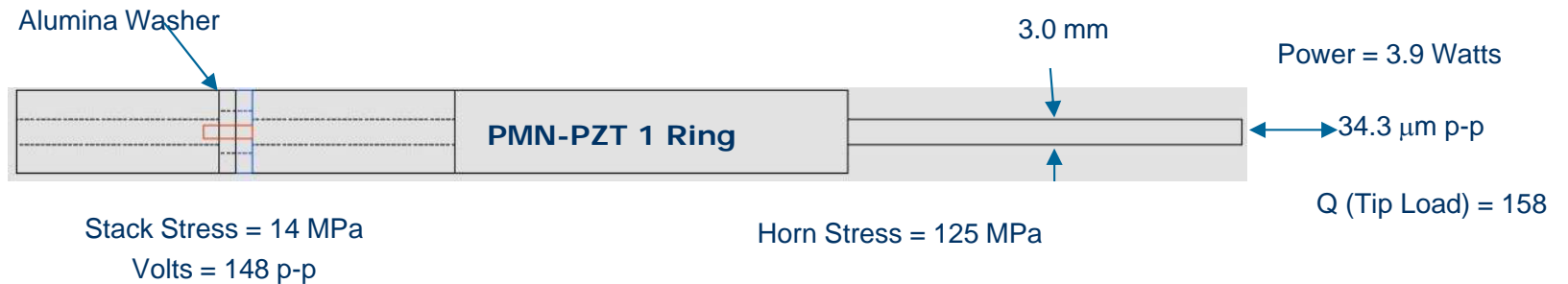
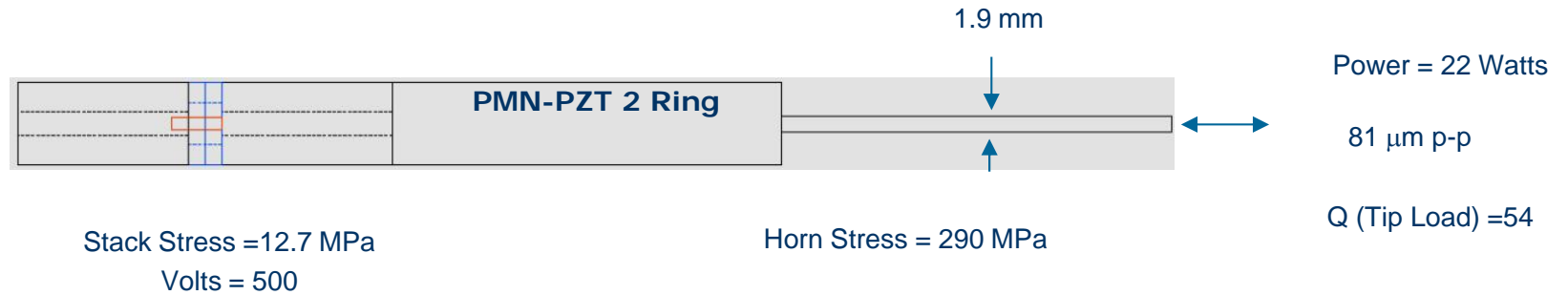
Heat Limit 41° C

- 26 kHz Resonant Frequency
 - Adjust End Mass Length
- 0.230 k_{eff}
 - Adjust Horn Gain



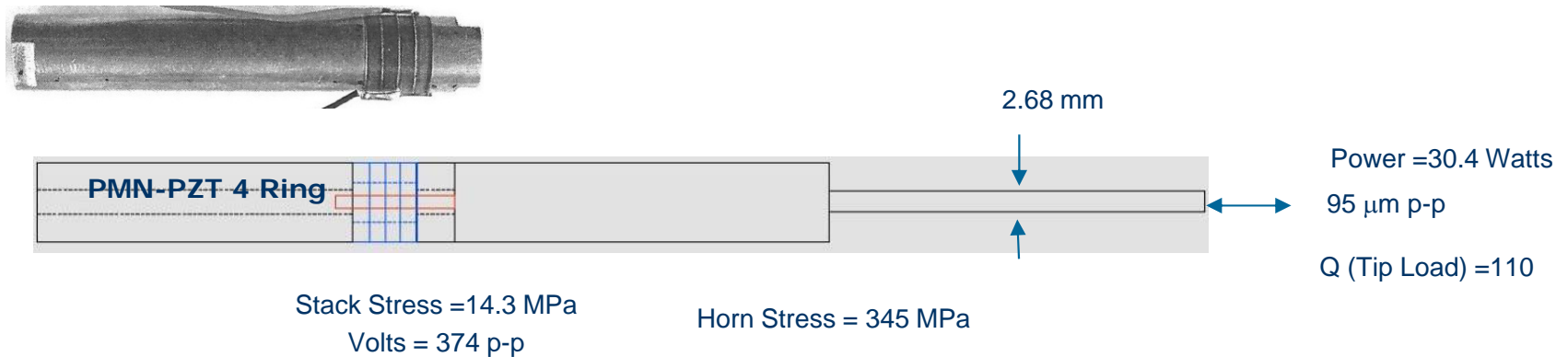
PMN-PZT 2 Ring Comparison With PMN-PZT 1 Ring

Heat Limit 40° C



PMN-PZT 7/8 Configuration

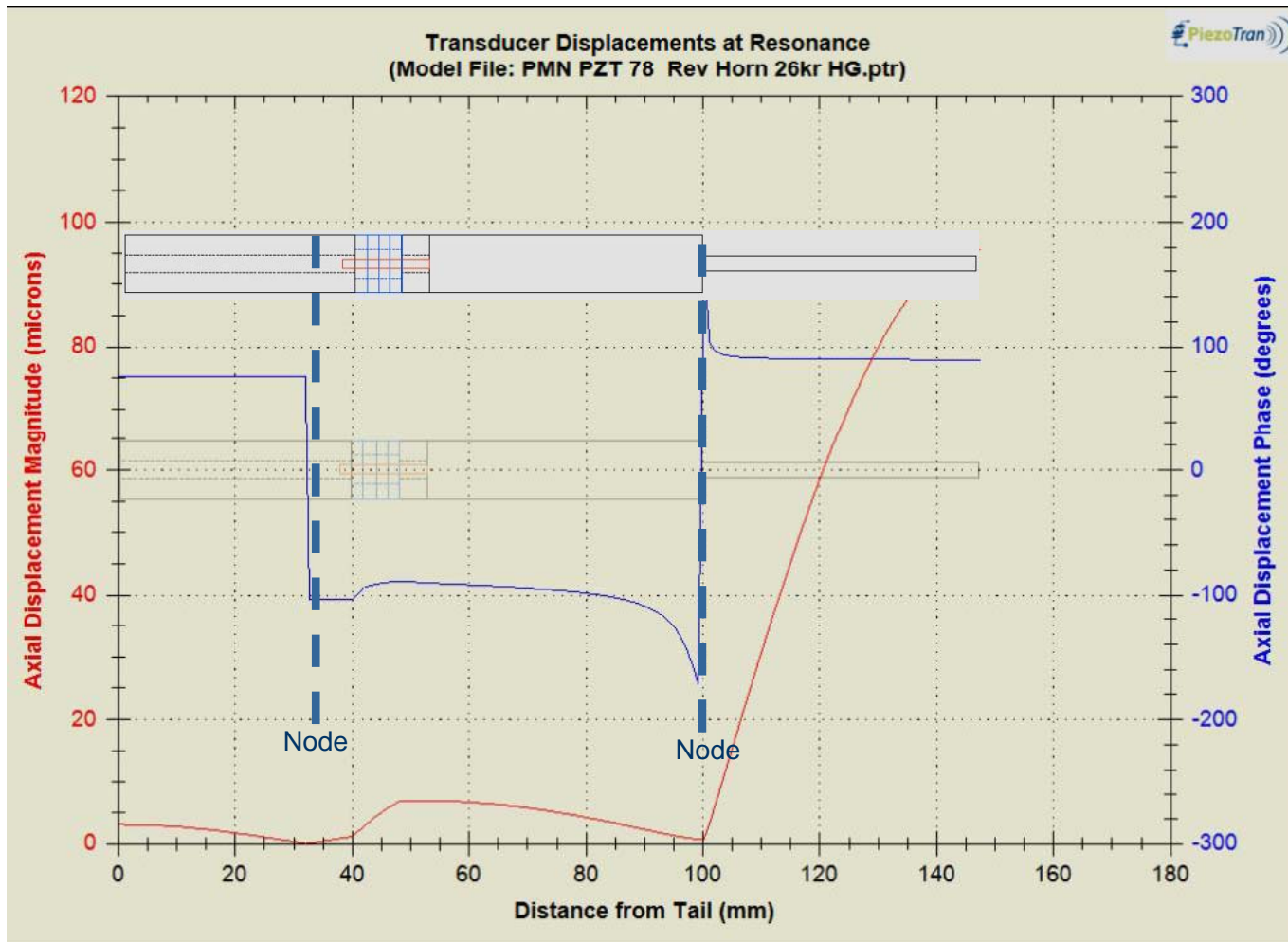
(Horn Attached to Rear Mass)



PMN-PZT 7/8 Configuration

(Horn Attached to Rear Mass)

Nodal Pattern



Tabulated Results

Resonant Frequency Tuned to 26 kHz by Adjusting End Mass Length
 K_{eff} 0.230 by Adjusting Horn Diameter

Transducer	Stroke μm p-p	Power (Watts)	Volts p-p	Q	Horn Stress MPa	Stack Stress MPa
4 Ring PZT8	29	2.84	51	1000	105	52.9
4 Ring PZT4	17.9	1.06	21	1478	64.5	35.9
PMN-PZT 7/8	95	30.4	374	110	345	14.3
PMN-PZT 2 Ring	81	22	500	54	290	12.7
PMN-PZT 1 Ring	34.3	3.9	148	158	125	14

Conclusions

- **Design Limitations**
 - Coupling Coefficient k_{eff} Related:
 - Primary Reserve Power
 - Secondary Horn Stress
 - Stack Heat Related:
 - Mechanical Q of the Piezo Rings and Joints
 - Location in the Stack
 - PZT8 Superior to PZT4
- **PMN-PZT**
 - Potentially Superior Performance
 - Customized Alternate Design Configurations
 - Dual Cascaded Horns, 2 Rings and 1Ring Piezo Stacks
 - Piezo Stacks Located Away From Nodes

Acknowledgments

Andrew Mathieson and Glasgow University

Primary Reference

“ The Influence of Piezoceramic Stack Location on Nonlinear Behavior of Langevin Transducers”

IEEE Transactions on Ultrasonics, Ferroelectrics and Frequency Control, Vol, 60, No6 , June 2013

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